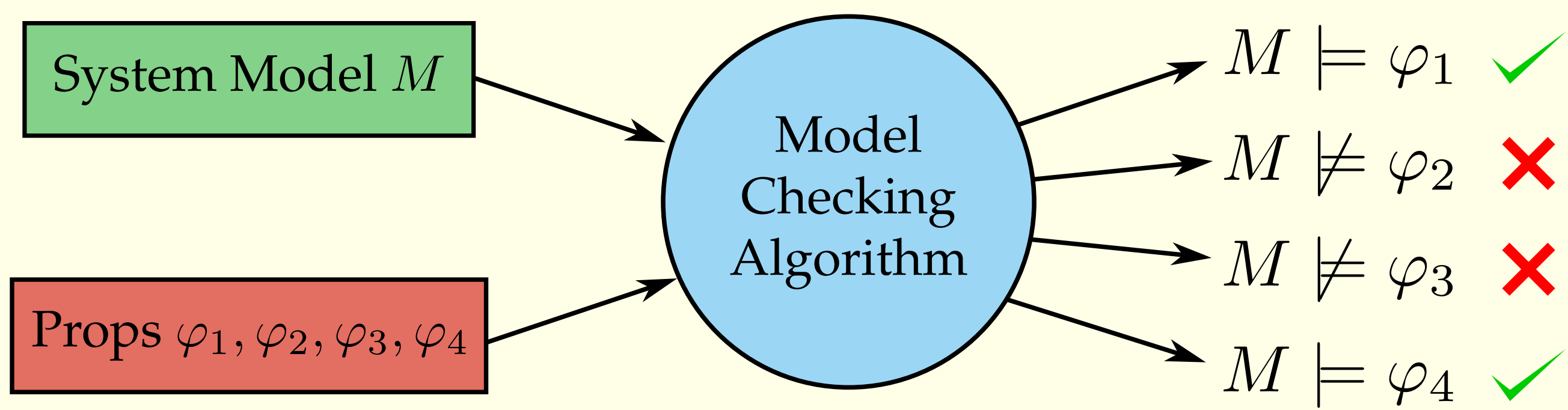


1. Motivation

- The formal verification of complex industrial designs often entails checking a large number of properties.

 - Equivalence checking** compares pairwise equality of each design output: distinct property per output,
 - Functional verification** checks low-level assertions to high-level encompassing properties, and
 - Design-space exploration** via model checking verifies properties against competing system designs.



- Most research and development efforts address the problem of single-property verification, multiple properties are verified concurrently, or one-at-a-time.

Possible inter-property relationships, and shared sub-problems are typically ignored.
Opportunity to save verification resource.

2. Multiple Property Verification

- Develop efficient and scalable techniques for automatic verification of multiple properties.

 - Inter-property relationships** – utilize logical dependencies to minimize model-checking runs.
 - Information reuse** – learned state-space information is reused across various property verification tasks.
 - Improved orchestration** – properties with nearly identical cone-of-influence are verified concurrently.

3. Inter-Property Relationships

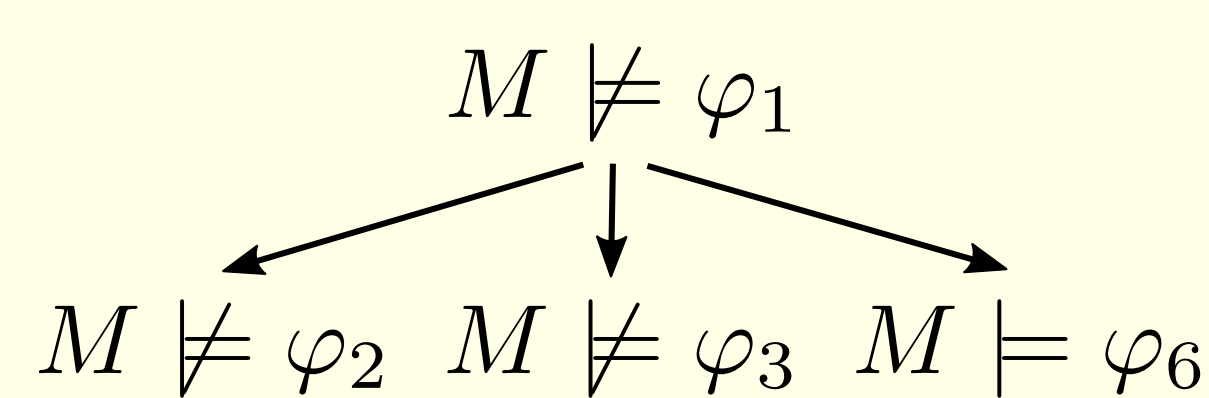
- Proprocess the set of properties to find pairwise logical dependencies; LTL satisfiability checking.

$$\varphi_1 = \Box p \quad \varphi_2 = \Box(p \wedge q) \quad \varphi_3 = \Box(p \vee q)$$

$M \models \varphi_2 \text{ then } M \models \varphi_1$ $M \models \varphi_2 \text{ then } M \models \varphi_3$
 φ_1 and φ_2 are dependent φ_2 and φ_3 are dependent

keys	dependencies
φ_1	φ_2 T, φ_3 T, φ_5 T
	φ_3 F
φ_2	φ_3 T, φ_4 T
	φ_1 F
φ_3	φ_1 T, φ_4 T
	φ_2 F, φ_6 T
	...

result
φ_1 F ✓
φ_2 F ✓
φ_3 F ✓
φ_4
φ_5
φ_6 T ✓
...



One check
Four results

Property Table

Result Array

Few minutes to find dependencies between properties, and <10% properties checked for each design.

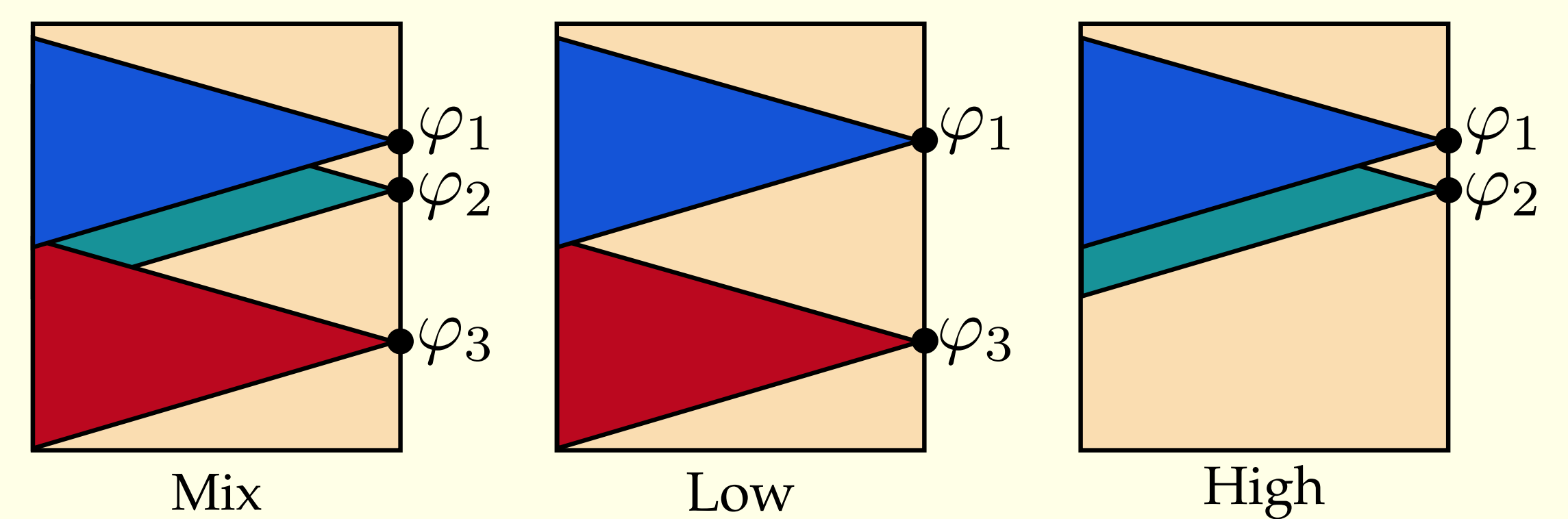
4. Information Reuse

- Sequentially check properties by reusing information; state approximations, counterexamples, and invariants.
- Stored information is repaired before reuse; add “just enough” extra information to enable reuse.

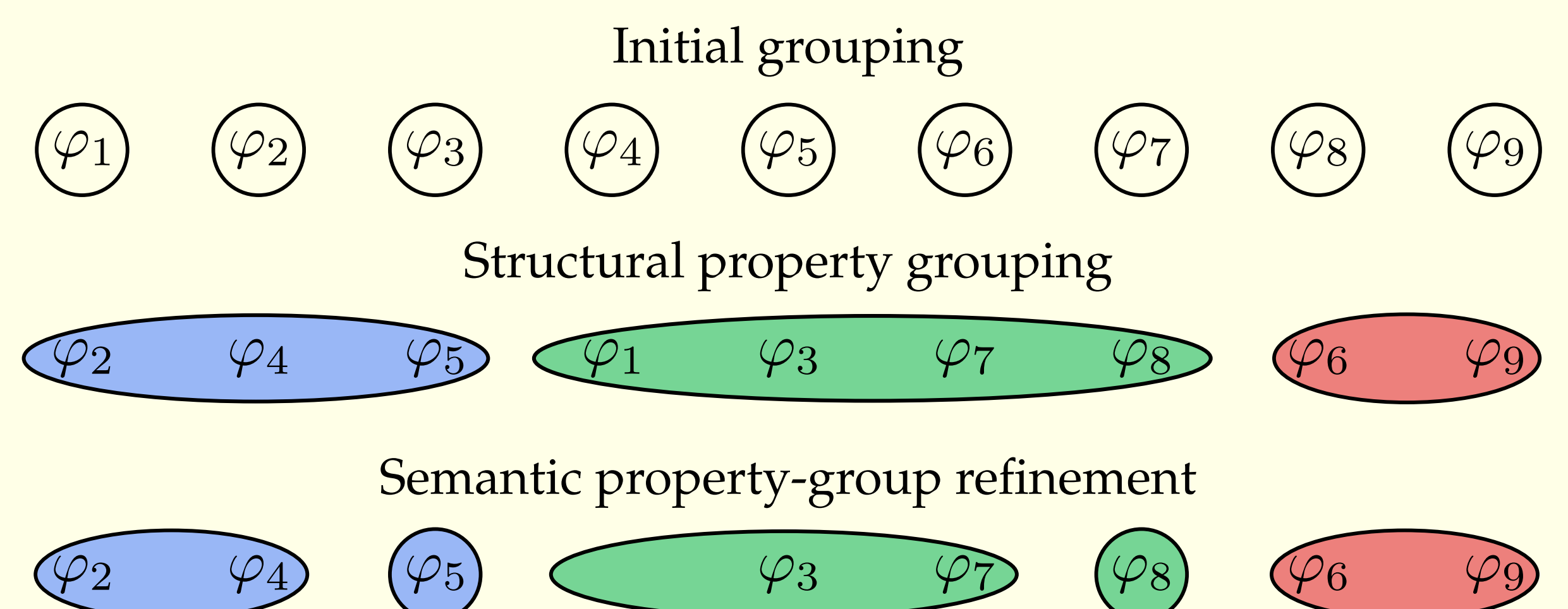
Adapt IC3/PDR for multi-property model checking by reusing frames to enable 4.5× faster verification.

5. Improved Orchestration

- Property grouping saves substantial verification resource by concurrent verification of high-affinity properties.



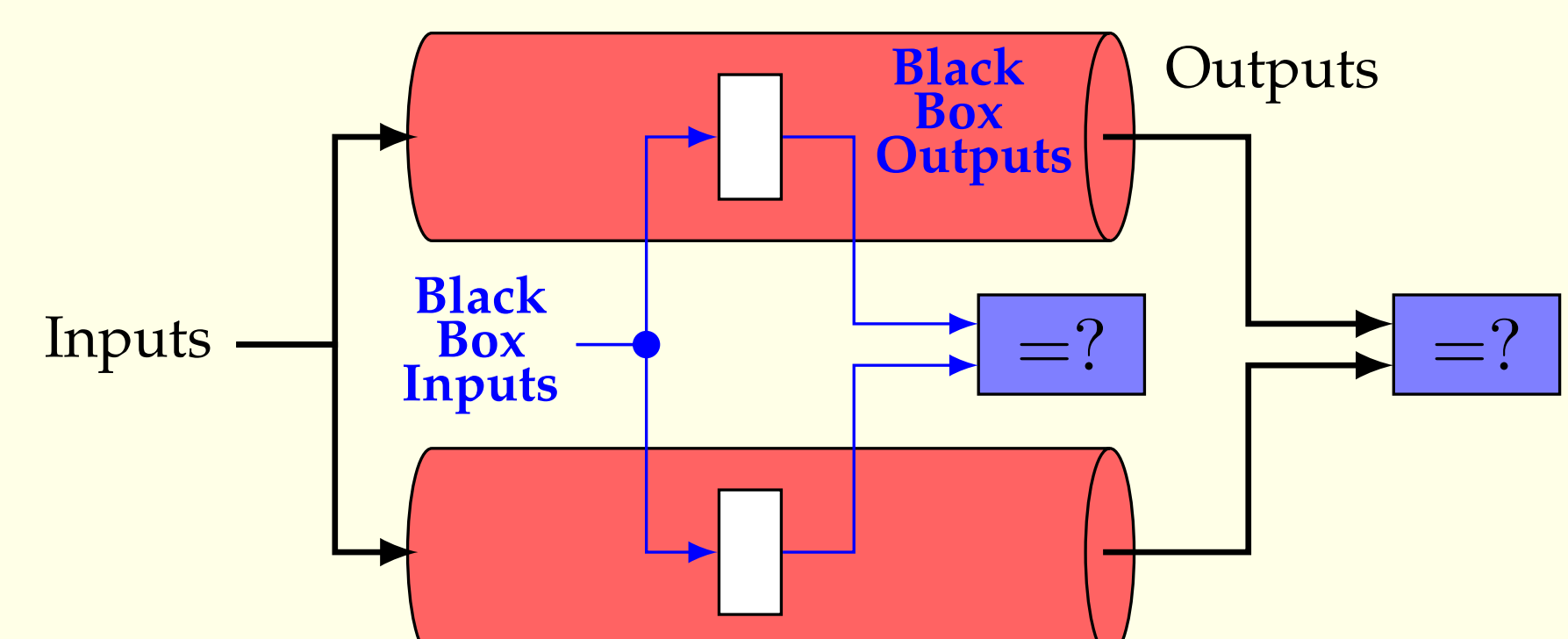
- Partition properties into provably high-affinity groups based on cone-of-influence (COI); ~linear runtime.
- Two-level orchestration; structural property grouping followed by semantic property-group refinement.



Improved multiple property verification offering 4.8× end-to-end speedup; advance state-of-the-art localization.

6. Ongoing and Future Work

- When to use structural vs. semantic grouping?** Difficult to discern what COI subset is relevant to what property.



- Sequential equivalence checking (SEC) is a prevalent multiple property verification application; several miters.
- Improve SEC by intelligently discharging non-inductive provable miters by improved property orchestration.

- “FuseIC3: An Algorithm for Checking Large Design Spaces,” in FMCAD, 2017.
- “More Scalable LTL Model Checking via Discovering Design-Space Dependencies,” in TACAS, 2018.
- “Boosting Verification Scalability via Structural Grouping and Semantic Partitioning of Properties,” in FMCAD, 2019.